

Outcome 2B Review Worksheet

CO#2B: Students will demonstrate understanding of irrational numbers in exponent form

Beginning	Approaching	Proficient	Mastery
I need help/I am inconsistent	I am consistently able to evaluate and simplify expressions using all exponent laws including a negative or rational exponent (numerical and variable bases) where there is one step	I am consistently able to simplify expressions by applying the exponent laws (numerical and variable bases) involving more than one step, including negative and rational exponents.	I am able to perform error analysis. I am able to determine which value is larger/smaller in a set of numbers. I am able to answer situational questions. I am able to explain my strategies.

Example 1

Given $16 = 2^4$ (Level 2)

- 4 is the exponent
- 2 is the base
- 16 is the standard (decimal) form
- 2^4 is the power
- $2 \times 2 \times 2 \times 2$ is repeated multiplication

1. For each of the following, determine:

- i) the exponent
- ii) the base
- iii) standard form
- iv) the power
- v) repeated multiplication

a) $8 = 2^3$ b) $5^2 = 25$ c) $16 = 4^2$ d) $2^5 = 32$

Example 2

When multiplying SAME bases you ADD exponents (Level 2)

a) $x^5 \times x^3$ b) $m^4 \times m^3 \times m$ c) $(-2)^3 \times (-2)^4$
 $= x^{5+3}$ $= m^{4+3+1}$ $= (-2)^{3+4}$
 $= x^8$ $= m^8$ $= (-2)^7$

2. Simplify the following:

a) $m^3 \times m^2$ b) $a^7 \times a$ c) $p^6 \times p^3 \times p^4$

d) $n^3 \times n^7 \times n$ e) $(-3)^4 \times (-3)^5$ f) $2^7 \times 2 \times 2^3$

g) $(-0.1)^4 (-0.1)^3$ h) $q^5 \times q^3 \times q \times q^6$ i) $k^3 \times k^7 \times k^2$

Example 3**When dividing same bases you SUBTRACT exponents (Level 2)**

a) $m^9 \div m^3$
 $= m^{9-3}$
 $= m^6$

b) $a^7 \div a$
 $= a^{7-1}$
 $= a^6$

c) $\frac{n^5}{n^3}$
 $= n^{5-3}$
 $= n^2$

d) $\frac{3^8}{3^5}$
 $= 3^{8-5}$
 $= 3^3$

3. Simplify the following

a) $m^{12} \div m^5$ b) $m^6 \div m^3$ c) $a^3 \div a$ d) $\frac{m^7}{m^3}$

e) $\frac{5^3}{5^2}$ f) $\frac{r^9}{r^6}$ g) $\frac{a^{15}}{a^3}$ h) $\frac{(-0.1)^5}{(-0.1)^3}$ i) $\frac{7^3}{7}$

Example 4**To raise a power to a power, you MULTIPLY exponents (Level 2)**

a) $(a^5)^3$
 $= a^{5 \times 3}$
 $= a^{15}$

b) $(3^2)^4$
 $= 3^{2 \times 4}$
 $= 3^8$

4. Simplify the following

a) $(m^5)^2$ b) $(a^3)^3$ c) $(4^2)^5$ d) $(3^3)^4$ e) $(p^7)^2$

Example 5**Exponent of zero gives a value of one (level 2)**

a) a^0 b) $(-a)^0$
 $= 1$ $= 1$

c) $-a^0$ d) $(2a)^0$
 $= -1$ $= 1$

e) $2a^0$
 $= 2$

5. Evaluate

a) $-m^0$ b) m^0 c) $(-m)^0$ d) $3m^0$ e) $-3m^0$

f) $(3m)^0$

g) $(-3m)^0$

Example 6 To change a negative exponent to a positive exponent, you determine the reciprocal (Level 2)

a) a^{-2}
 $= \frac{1}{a^2}$

b) m^{-5}
 $= \frac{1}{m^5}$

c) 3^{-4}
 $= \frac{1}{3^4}$

6. Write with a positive exponent

a) m^{-3} b) a^{-7} c) n^{-9} d) p^{-1} e) 2^{-5} f) 3^{-6}

g) $(-4)^{-9}$ h) a^{-10} i) b^{-12} j) k^{-11} k) 7^{-3} l) $(-5)^{-3}$

Example 7 (Level 2)

a) $\frac{1}{5^{-2}}$ b) $\frac{1}{m^{-3}}$ c) $\frac{1}{a^{-4}}$
 $= 5^2$ $= m^3$ $= a^4$

7. Write with a positive exponent

a) $\frac{1}{a^{-5}}$ b) $\frac{1}{a^{-6}}$ c) $\frac{1}{m^{-2}}$ d) $\frac{1}{2^{-4}}$ e) $\frac{1}{3^{-5}}$ f) $\frac{1}{4^{-2}}$

Example 8 Simplify and write with positive exponents (Level 3)

a) $a^7 \times a^{-5} \times a^{-4}$ b) $m^5 \times m^{-7}$ c) $n^{-3} \times n^{-2}$
 $= a^{7+(-5)+(-4)}$ $= m^{5+(-7)}$ $= n^{-3+(-2)}$
 $= a^{-2}$ $= m^{-2}$ $= n^{-5}$
 $= \frac{1}{a^2}$ $= \frac{1}{m^2}$ $= \frac{1}{n^5}$

8. Simplify and write with positive exponents

a) $m^3 \times m^{-6}$ b) $a^{-3} \times a$ c) $q^{-5} \times q^3 \times q^{-4}$ d) $m^2 \times m^{-5} \times m^{-1}$

Example 9 Simplify and write with positive exponents (Level 3)

a) $n^2 \div n^5$ b) $n^{-4} \div n^2$ c) $n^3 \div n^{-4}$ d) $n^{-5} \div n^{-2}$
 $= n^{2-5}$ $= n^{-4-2}$ $= n^{3-(-4)}$ $= n^{-5-(-2)}$
 $= n^{-3}$ $= n^{-6}$ $= n^7$ $= n^{-3}$
 $= \frac{1}{n^3}$ $= \frac{1}{n^6}$ $= \frac{1}{n^3}$

9. Simplify and write with positive exponents

a) $m^3 \div m^5$ b) $a^7 \div a^9$ c) $a^{-4} \div a^3$ d) $a^{-2} \div a$

e) $m^{-3} \div m^5$ f) $n^5 \div n^{-2}$ g) $n^3 \div n^{-4}$ h) $n^5 \div n^{-9}$

i) $n^{-4} \div n^{-2}$ j) $n^{-3} \div n^{-5}$ k) $n^{-2} \div n^{-3}$ l) $n^{-1} \div n^{-4}$

Example 10 Simplify and write with positive exponents (Level 3)

a) $\frac{m^3 \times m^4}{m^9}$	b) $\frac{a^{-2} \times a^4}{a^{-3}}$	c) $(m^5 n^2)^3$	d) $(a^{-2} b^{-3})^2$
$= m^{3+4-9}$	$= a^{-2+4-(-3)}$	$= m^{5 \times 3} n^{2 \times 3}$	$= a^{-2 \times 2} b^{-3 \times 2}$
$= m^{-2}$	$= a^5$	$= m^{15} n^6$	$= a^{-4} b^{-6}$
$= \frac{1}{m^2}$			$= \frac{1}{a^4 b^6}$
e) $(m^3 n^2)^{-4}$	f) $(a^3 b^{-2})^4$	g) $\frac{a^3}{b^{-2}}$	h) $\frac{a^{-3}}{b^2}$
$= m^{3 \times -4} n^{2 \times -4}$	$= a^{3 \times 4} b^{-2 \times 4}$	$= a^3 b^2$	$= \frac{1}{a^3 b^2}$
$= m^{-12} n^{-8}$	$= a^{12} b^{-8}$		
$= \frac{1}{m^{12} n^8}$	$= \frac{a^{12}}{b^8}$		

10. Simplify and write with positive exponents.

a) $\frac{n^5 n^2}{n^6}$ b) $\frac{n^3 n^4}{n^{10}}$ c) $\frac{n^{-2} n^{-3}}{n^{-5}}$ d) $\frac{n^{-1} n^3}{n^{-5}}$ e) $\frac{n^{-2} n^{-2}}{n^5}$ f) $(a^2 b^5)^3$

g) $(m^3 n^2)^5$ h) $(a^4 b)^7$ i) $(m^2 n)^5$ j) $(a^{-3} b^{-4})^2$ k) $(m^{-1} n^{-2})^3$ l) $(m^{-4} n^{-3})^2$

$$\text{m)} \quad (m^{-2}n^{-3})^4 \quad \text{n)} \quad (a^2b^5)^{-1} \quad \text{o)} \quad (a^3b^4)^{-2} \quad \text{p)} \quad (m^7n^3)^{-5} \quad \text{q)} \quad (a^5b^2)^{-3} \quad \text{r)} \quad (s^5t^3)^{-2}$$

$$\text{s)} \quad (m^5n^{-2})^4 \quad \text{t)} \quad (a^{-3}b^4)^5 \quad \text{u)} \quad (m^4n^{-2})^3 \quad \text{v)} \quad (a^{-7}b^4)^2 \quad \text{w)} \quad (m^{-3}n^2)^{-4} \quad \text{x)} \quad (a^{-2}b^1)^{-4}$$

$$\text{y)} \quad \frac{a^5}{b^{-3}} \quad \text{z)} \quad \frac{m^7}{n^{-5}} \quad \text{aa)} \quad \frac{b^8}{c^{-4}} \quad \text{bb)} \quad \frac{d^7}{e^{-2}} \quad \text{cc)} \quad \frac{f^3}{g^{-5}} \quad \text{dd)} \quad \frac{h^9}{i^{-3}}$$

$$\text{ee)} \quad \frac{a^{-3}}{b^4} \quad \text{ff)} \quad \frac{c^{-2}}{d^8} \quad \text{gg)} \quad \frac{e^{-4}}{f^5} \quad \text{hh)} \quad \frac{g^{-3}}{h^5} \quad \text{ii)} \quad \frac{j^{-7}}{k^3} \quad \text{jj)} \quad \frac{m^{-5}}{n^4}$$

Example 11 Evaluate (level 2)

a)	2^3	b)	-2^3	c)	$(-2)^3$	d)	-2^4	e)	$(-2)^4$
	$=2 \times 2 \times 2$		$=-2 \times 2 \times 2$		$=-2 \times -2 \times -2$		$=-2 \times 2 \times 2 \times 2$		$=-2 \times -2 \times -2 \times -2$
	$=8$		$=-8$		$=-8$		$=-16$		$=16$

11. Evaluate

$$\text{a)} \quad 4^2 \quad \text{b)} \quad -4^2 \quad \text{c)} \quad (-4)^2 \quad \text{d)} \quad 4^3 \quad \text{e)} \quad -4^3 \quad \text{f)} \quad (-4)^3$$

$$\text{g)} \quad 3^2 \quad \text{h)} \quad -3^2 \quad \text{i)} \quad (-3)^2 \quad \text{j)} \quad 3^3 \quad \text{k)} \quad -3^3 \quad \text{l)} \quad (-3)^3$$

m) 5^2 n) -5^2 o) $(-5)^2$ p) 5^3 q) -5^3 r) $(-5)^3$

Example 12 Evaluate (Level 2)

a) 2^{-3}	b) -2^{-3}	c) $(-2)^{-3}$	d) -2^{-4}	e) $(-2)^{-4}$
$= \frac{1}{2^3}$	$= \frac{1}{-2^3}$	$= \frac{1}{(-2)^3}$	$= \frac{1}{-2^4}$	$= \frac{1}{(-2)^4}$
$= \frac{1}{8}$	$= \frac{1}{-8}$	$= \frac{1}{-8}$	$= \frac{1}{-16}$	$= \frac{1}{16}$
		$= \frac{-1}{8}$	$= \frac{-1}{16}$	

12. Evaluate (Do NOT write your answer as a decimal)

a) 4^{-3} b) -4^{-3} c) $(-4)^{-3}$ d) -4^{-4} e) $(-4)^{-4}$ f) 4^{-4}

g) 3^{-3} h) 3^{-3} i) $(-3)^{-3}$ j) -3^{-4} k) $(-3)^{-4}$ l) 3^{-4}

m) 5^{-2} n) -5^{-2} o) $(-5)^{-2}$ p) -5^{-3} q) $(-5)^{-3}$ r) 5^{-3}

Example 13 Write each power as a radical (Level 2). The denominator ends up as the index (inside the “hook”) and the numerator becomes the exponent. Keep in mind an exponent of 1 doesn’t show the 1, and a square root does not have to put the 2 in the “hook”.

a) $\sqrt[3]{7}$	b) $\sqrt[5]{25}$	c) $\sqrt[3]{125}$	d) $\sqrt[4]{64}$
$\sqrt[3]{7}$	$\sqrt[5]{25}$	$\sqrt[3]{125}$	$\sqrt[4]{64}$

13. Write each power as a radical

a) $40^{\frac{3}{5}}$ b) $26^{\frac{1}{3}}$ c) $49^{\frac{2}{3}}$ d) $15^{\frac{1}{4}}$ e) $80^{\frac{4}{5}}$

Example 14 Write each radical as a power (Level 2). The number in the “hook” goes in the denominator, the exponent goes in the numerator.

a) $\sqrt[3]{12}^{\frac{1}{2}}$

b) $\sqrt[5]{65}^{\frac{3}{2}}$

c) $\sqrt{20}^{\frac{1}{2}}$

d) $\sqrt[4]{56}^{\frac{3}{4}}$

14. Write each radical as a power.

a) $\sqrt[4]{75}^{\frac{3}{2}}$

b) $\sqrt[3]{18}^2$

c) $\sqrt[3]{15}$

d) $\sqrt{28}$

e) $\sqrt[3]{14}^3$

Example 15 Evaluate (Level 2). Write in radical form and then evaluate.

a) $81^{\frac{5}{2}}$
 $\sqrt{81}^3$
 9^3
 729

b) $27^{\frac{3}{2}}$
 $\sqrt[3]{27}^2$
 3^2
 9

c) $81^{\frac{5}{4}}$
 $\sqrt[4]{81}^3$
 3^3
 27

15. Evaluate

a) $27^{\frac{2}{3}}$

b) $25^{\frac{1}{2}}$

c) $125^{\frac{2}{3}}$

d) $256^{\frac{5}{4}}$

e) $81^{\frac{5}{4}}$

Example 16 Simplify. Write answers with positive exponents (Level 3)

a) $(3a)^2$
 $=3^2a^2$
 $=9a^2$

b) $(-2m^{-3}n^{2/3})^3$
 $=-2^3m^{3 \times 3}n^{2 \times 3}$
 $=-8m^9n^6$

c) $(3mn^2)^{-2}$
 $=3^{-2}m^{-2}n^{2 \times -2}$
 $=3^{-2}m^{-2}n^{-4}$
 $\frac{1}{3^2m^2n^2}$
 $=\frac{1}{9m^2n^2}$

16. Simplify. Write answers with positive exponents

a) $(5m)^3$

b) $(-4a^3b^5)^5$

c) $(2ab^5)^{-3}$

d) $(3m^3n)^{-2}$

Example 17 Simplify. Write all answers with positive exponents (Level 3)

a) $\left[\frac{4a^{-5}}{9b^{-3}} \right]^{-2}$

$$\begin{aligned} & \frac{4^{-2}a^{-5 \times -2}}{9^{-2}b^{-3 \times -2}} \\ & \frac{4^{-2}a^{10}}{9^{-2}b^6} \\ & \frac{9^2a^{10}}{4^2b^6} \end{aligned}$$

$$\frac{81a^{10}}{16b^6}$$

17. Simplify. Write all answers with positive exponents

a) $\left[\frac{2a^{-5}}{3b^{-3}} \right]^{-3}$

b) $\left[\frac{4a^{-3}}{9b^{-4}} \right]^2$

c) $\left[\frac{2a^{-5}}{3b^2} \right]^{-4}$

d) $\left[\frac{4a^{-5}b^2}{9a^{-7}b^{-3}} \right]^{-2}$

e) $\left[\frac{2a^{-5}b^{-5}}{5a^7b^{-3}} \right]^3$

f) $\left[\frac{5a^{-5}b^5c^{-3}}{9a^{-6}b^{-3}c^{-7}} \right]^2$

Example 18 Simplify. Write all answers with positive exponents. (Level 3)

a) $\left(\frac{2^2}{9}\right)^{-\frac{1}{2}}$

$$\frac{2^{2 \times -\frac{1}{2}}}{9^{\frac{1}{2}}} =$$

$$\frac{2^{-1}}{9^{\frac{1}{2}}} =$$

$$\frac{\frac{1}{2}}{9^{\frac{1}{2}}} =$$

$$\frac{\frac{1}{2}}{3} =$$

$$\frac{1}{2}$$

b) $(x^{\frac{5}{4}}y)(x^{\frac{2}{4}}y^{-4})$

$$x^{\frac{5}{4} + \frac{2}{4}}y^{1+(-4)} =$$

$$x^{\frac{7}{4}}y^{-3} =$$

$$\frac{x^{\frac{7}{4}}}{y^3} =$$

c) $81^{-\frac{3}{4}}$

$$\frac{1}{81^{\frac{3}{4}}} =$$

$$\frac{1}{\sqrt[4]{81^3}} =$$

$$\frac{1}{3^6} =$$

$$\frac{1}{27} =$$

18. Simplify. Write all answers with positive exponents.

a) $\left(\frac{4^4}{25}\right)^{-\frac{1}{2}}$

b) $(x^{\frac{1}{5}}y)(x^{\frac{2}{5}}y^{-3})$

c) $16^{-\frac{3}{4}}$

Level 4

The rubric states: I am able to perform error analysis. I am able to determine which value is larger/smaller in a set of numbers. I am able to answer situational questions. I am able to explain my strategies.

Go through your practice assignments to review these types of questions.