

Math 10 Foundations Final Review

*Does not include level 4 questions. Does not include outcomes 3a and 3b

Outcomes 1A

Level 2

1. Write the prime factorization of 168

$$\begin{array}{r}
 168 \\
 \wedge \\
 8 \quad 21 \\
 \wedge \quad \wedge \\
 4 \quad 3 \quad 7 \\
 \wedge \quad \wedge \\
 2 \quad 2 \quad 3 \quad 7 \\
 \wedge \quad \wedge \\
 2 \quad 2
 \end{array}
 \qquad
 168 = 2 \cdot 2 \cdot 2 \cdot 3 \cdot 7$$

OR

$$= 2^3 \cdot 3 \cdot 7$$

2. Find the GCF and the LCM of 40 and 64

$$\begin{array}{l}
 40 = 2 \cdot 2 \cdot 2 \cdot 5 \\
 64 = 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2
 \end{array}
 \qquad
 \begin{array}{l}
 \text{LCM} = 2^6 \cdot 5 \\
 = 320
 \end{array}$$

$$\text{GCF} = 2 \cdot 2 \cdot 2 = 8$$

3. Find the GCF and LCM of 6 and 10

$$\begin{array}{l}
 6 = 2 \cdot 3 \\
 10 = 2 \cdot 5
 \end{array}
 \qquad
 \begin{array}{l}
 \text{LCM} = 2 \cdot 3 \cdot 5 \\
 = 30
 \end{array}$$

$$\text{GCF} = 2$$

Level 3

4. Find the square root (without using the $\sqrt{\quad}$ button on your calculator). Show your work.

a) 576

$$\begin{array}{r}
 576 \\
 \wedge \\
 24 \quad 24 \\
 \wedge \quad \wedge \\
 4 \quad 6 \quad 4 \quad 6 \\
 \wedge \quad \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 2 \quad 2 \quad 3 \quad 3
 \end{array}$$

$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 3 \cdot 3} = 2 \cdot 2 \cdot 2 \cdot 3 = 24$$

b) 8100

$$\begin{array}{r}
 8100 \\
 \wedge \\
 90 \quad 90 \\
 \wedge \quad \wedge \\
 3 \quad 3 \quad 3 \quad 3 \quad 5 \quad 5
 \end{array}$$

$$\sqrt{2 \cdot 2 \cdot 3 \cdot 3 \cdot 3 \cdot 3 \cdot 5 \cdot 5} = 2 \cdot 3 \cdot 3 \cdot 5 = 90$$

$$\begin{array}{r}
 8100 \\
 \wedge \\
 9 \quad 900 \\
 \wedge \quad \wedge \\
 3 \quad 3 \quad 3 \quad 300 \\
 \wedge \quad \wedge \\
 3 \quad 100 \\
 \wedge \quad \wedge \\
 10 \quad 10 \\
 \wedge \quad \wedge \\
 2 \quad 5 \quad 2 \quad 5
 \end{array}$$

5. Find the cube root (without using the $\sqrt[3]{\quad}$ button on your calculator). Show your work.

a) 4096

$$\begin{array}{r}
 4096 \\
 \wedge \\
 8 \quad 512 \\
 \wedge \quad \wedge \\
 2 \quad 4 \quad 128 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 4 \quad 32 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 4 \quad 8 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 2 \quad 2 \quad 2
 \end{array}$$

$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2} = 2 \cdot 2 \cdot 2 \cdot 2 = 16$$

b) 512

$$\begin{array}{r}
 512 \\
 \wedge \\
 4 \quad 128 \\
 \wedge \quad \wedge \\
 2 \quad 4 \quad 32 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 4 \quad 8 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 2 \quad 2 \quad 2
 \end{array}$$

$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2} = 2 \cdot 2 \cdot 2 = 8$$

$$\begin{array}{r}
 512 \\
 \wedge \\
 4 \quad 128 \\
 \wedge \quad \wedge \\
 2 \quad 4 \quad 32 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 4 \quad 8 \\
 \wedge \quad \wedge \quad \wedge \\
 2 \quad 2 \quad 2 \quad 2 \quad 2
 \end{array}$$

Outcome 2a

Level 2/3

6. Write each mixed radical as an entire radical

$$\begin{aligned} \text{a) } 12\sqrt{3} &= \sqrt{12 \cdot 12 \cdot 3} \\ &= \sqrt{432} \end{aligned}$$

$$\begin{aligned} \text{b) } 3\sqrt[3]{7} &= \sqrt[3]{3 \cdot 3 \cdot 3 \cdot 7} \\ &= \sqrt[3]{189} \end{aligned}$$

$$\begin{aligned} \text{c) } 2\sqrt[5]{15} &= \sqrt[5]{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 15} \\ &= \sqrt[5]{480} \end{aligned}$$

7. Write each as a mixed radical in simplest form.

$$\begin{aligned} \text{a) } \sqrt{45} &= \sqrt{9 \cdot 5} \\ &= 3\sqrt{5} \end{aligned}$$

$$\begin{aligned} \text{b) } \sqrt[3]{128} &= \sqrt[3]{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 2} \\ &= 2 \cdot 2\sqrt[3]{2} \\ &= 4\sqrt[3]{2} \end{aligned}$$

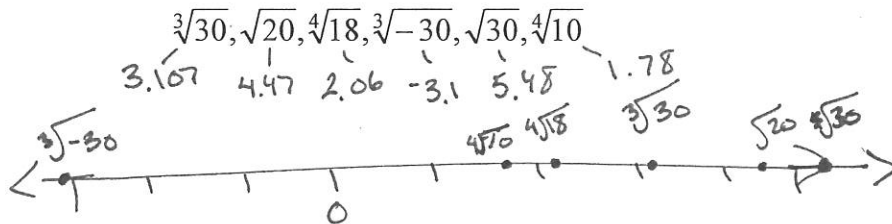
$$\begin{aligned} \text{c) } \sqrt{539} &= \sqrt{7 \cdot 7 \cdot 11} \\ &= 7\sqrt{11} \end{aligned}$$

$$\begin{aligned} \text{d) } \sqrt{80} &= \sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 5} \\ &= 2 \cdot 2\sqrt{5} \\ &= 4\sqrt{5} \end{aligned}$$

$$\begin{aligned} \text{e) } \sqrt{75} &= \sqrt{25 \cdot 3} \\ &= 5\sqrt{3} \end{aligned}$$

$$\begin{aligned} \text{d) } \sqrt[3]{108} &= \sqrt[3]{2 \cdot 2 \cdot 3 \cdot 3 \cdot 3} \\ &= 3\sqrt[3]{4} \end{aligned}$$

8. Place each number on a number line, and then order the numbers from least to greatest.



9. Determine if the following are rational or irrational. Explain how you know.

$$\begin{aligned} \text{a) } \sqrt{26} &= \sqrt{2 \cdot 13} \\ &= \sqrt{26} \end{aligned}$$

Irrational

$$\begin{aligned} \text{b) } \sqrt[3]{81} &= \sqrt[3]{3 \cdot 3 \cdot 3 \cdot 3} \\ &= 3\sqrt[3]{3} \end{aligned}$$

Irrational

Outcome 2b

Level 2

10. Rewrite the following with positive exponents only

a) x^{-3}
 $= \frac{1}{x^3}$

b) $\frac{1}{d^{-4}}$
 $= d^4$

c) $\left(\frac{a}{b}\right)^{-2}$
 $= \frac{a^{-2}}{b^{-2}} = \frac{b^2}{a^2}$ or $\left(\frac{b}{a}\right)^2$

11. Rewrite the following as a radical. Do not evaluate

a) $(-8)^{\frac{5}{3}}$
 $= \sqrt[3]{(-8)^5}$

b) $48^{\frac{1}{2}}$
 $= \sqrt{48}$

c) $25^{\frac{3}{4}}$
 $= \sqrt[4]{25^3}$
 $= \sqrt[4]{25^3}$

d) $7^{-\frac{1}{3}}$
 $= \frac{1}{7^{\frac{1}{3}}} = \frac{1}{\sqrt[3]{7}}$

12. Rewrite the following as an exponent. Do not evaluate

a) $\sqrt[3]{4}$
 $= 4^{\frac{1}{3}}$

b) $(\sqrt{5})^3$
 $= 5^{\frac{3}{2}}$

c) $\sqrt[4]{x^3}$
 $= x^{\frac{3}{4}}$

13. Write as a single power.

a) $y^3 y^2$
 $= y^5$

b) $\frac{a^6}{a^2}$
 $= a^4$

c) $(d^7)^2$
 $= d^{14}$

14. Evaluate the following. NO DECIMAL ANSWERS

a) 3^{-2}
 $= \frac{1}{3^2} = \frac{1}{9}$

b) 4^{-3}
 $= \frac{1}{4^3} = \frac{1}{64}$

level 3

c) $(27)^{\frac{2}{3}}$
 $= \sqrt[3]{27^2}$
 $= 3^2$
 $= 9$

d) $27^{-\frac{1}{3}}$
 $= \frac{1}{27^{\frac{1}{3}}} = \frac{1}{\sqrt[3]{27}}$
 $= \frac{1}{3}$

15. Simplify the following with positive exponents only.

$$\begin{aligned} \text{a) } m^{-7} \times m^3 \\ = m^{-4} \\ = \frac{1}{m^4} \end{aligned}$$

$$\begin{aligned} \text{b) } \frac{a^3}{a^{-8}} \\ = a^{11} \end{aligned}$$

$$\begin{aligned} \text{c) } (x^2 y^{-3})^4 \\ = x^8 y^{-12} \\ = \frac{x^8}{y^{12}} \end{aligned}$$

$$\begin{aligned} \text{d) } (a^3 b)(a^{-1} b^4) \\ = \cancel{a^3} \cancel{b^4} \\ = \frac{b^4}{a^3} \\ = a^2 b^5 \end{aligned}$$

$$\begin{aligned} \text{e) } \frac{x^2 y}{x^3 y^{-2}} \\ = \frac{y^3}{x} \end{aligned}$$

$$\begin{aligned} \text{f) } \left(\frac{x^2 y}{y^{-2}} \right)^{-2} \\ = \frac{x^4 y^{-2}}{y^{-4}} \\ = \frac{x^4}{y^6} \\ = \frac{1}{x^4 y^6} \end{aligned}$$

$$\begin{aligned} \text{g) } (3m^4 n)^2 \\ = 3^2 m^8 n^2 \\ = 9m^8 n^2 \end{aligned}$$

$$\begin{aligned} \text{h) } (m^2 n^{-4})^{-2} \\ = m^{-4} n^8 \\ = \frac{n^8}{m^4} \end{aligned}$$

$$\begin{aligned} \text{g) } (g^{\frac{2}{3}} h^{-\frac{3}{4}}) (g^{\frac{1}{4}} h^{\frac{1}{2}}) \\ = g^{\frac{11}{12}} h^{-\frac{1}{4}} \\ = \frac{g^{\frac{11}{12}}}{h^{\frac{1}{4}}} \end{aligned}$$

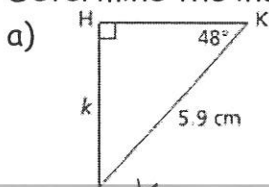
$$\begin{aligned} \text{h) } (x^{-\frac{2}{5}})^{\frac{2}{3}} \\ = x^{-\frac{4}{15}} \\ = \frac{1}{x^{\frac{4}{15}}} \end{aligned}$$

$$\begin{aligned} \text{i) } \left(\frac{4x^4}{9x^3} \right)^{\frac{1}{2}} \\ = 4^{-\frac{1}{2}} x^{-\frac{3}{8}} \\ = \frac{9^{-\frac{1}{2}} x^{-\frac{3}{2}}}{4^{\frac{1}{2}} x^{\frac{3}{8}}} \\ = \frac{9^{\frac{1}{2}} x^{\frac{3}{2}}}{4^{\frac{1}{2}} x^{\frac{3}{8}}} = \frac{3x^{\frac{3}{2}}}{2x^{\frac{3}{8}}} \end{aligned}$$

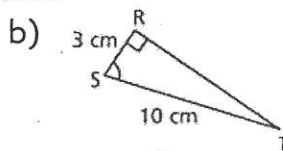
Outcome 4

level 2/3

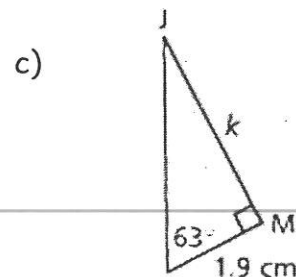
16. Determine the indicated measurement



$$\begin{aligned} \sin 48 &= \frac{k}{5.9} \\ k &= (\sin 48)(5.9) \\ k &= 4.38 \text{ cm} \end{aligned}$$

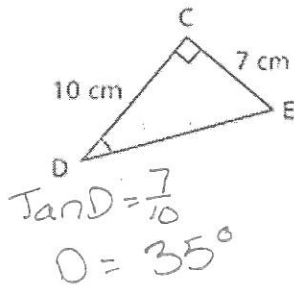


$$\begin{aligned} \cos S &= \frac{3}{10} \\ S &= 72.5^\circ \end{aligned}$$

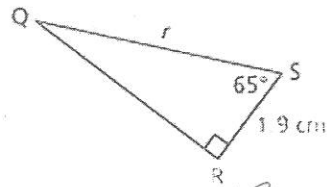


$$\begin{aligned} \tan 63 &= \frac{k}{1.9} \\ k &= (\tan 63)(1.9) \\ k &= 2.72 \text{ cm} \end{aligned}$$

d)



e)

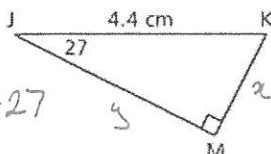


$\cos 65 = \frac{1.9}{r}$
 $\frac{1.9}{\cos 65} = \frac{(\cos 65)(r)}{\cos 65}$
 $r = 4.5 \text{ cm}$

Level 4

17. Solve the triangle

a)

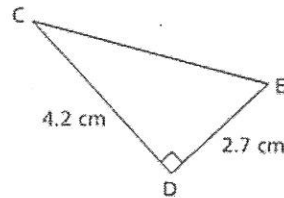


$\angle K = 180 - 90 - 27$
 $= 63^\circ$

$\text{KM} \rightarrow \sin 27 = \frac{x}{4.4}$
 $x = 2.0 \text{ cm}$

$\text{JM} \rightarrow \cos 27 = \frac{y}{4.4}$
 $y = 3.9 \text{ cm}$

b)



$\text{CE} \rightarrow 4.2^2 + 2.7^2 = c^2$
 $17.64 + 7.29 = c^2$
 $24.93 = c^2$
 $c = 4.99 \text{ cm}$

$\text{LC} \rightarrow \tan C = \frac{2.7}{4.2}$
 $C = 32.7^\circ$

$\text{LE} \rightarrow 180 - 90 - 32.7$
 $= 57.3^\circ$

Outcome 5A

18. Expand and Simplify

a) $(9 + m)(9 + m)$

$= 81 + 9m + 9m + m^2$

$= 81 + 18m + m^2$

b) $(3a - 5)(2a - 3)$

$= 6a^2 - 9a - 10a + 15$

$= 6a^2 - 19a + 15$

c) $(2n + 3p)(5n - 4p)$

$= 10n^2 - 8np + 15np - 12p^2$

$= 10n^2 + 7np - 12p^2$

d) $(w + 4)(-2w^2 + 7w - 8)$

$= -2w^3 + 7w^2 - 8w - 8w^2 + 28w - 32$

$= -2w^3 - w^2 + 20w - 32$

$$e) (4 + 3x - 2x^2)(-2 + 2x + 3x^2)$$

$$= -8 + 8x + 12x^2 - 6x + 6x^2 + 9x^3 + 4x^2 - 4x^3 - 6x^4$$

$$= -6x^4 + 5x^3 + 22x^2 + 2x - 8$$

$$f) (2m + 3n - 5)(3m - 4n)$$

$$= 6m^2 - 8mn + 9mn - 12n^2 - 15m + 20n$$

$$= 6m^2 - 12n^2 + mn - 15m + 20n$$

$$g) (3x - 2)^2$$

$$= (3x - 2)(3x - 2)$$

$$= 9x^2 - 6x - 6x + 4$$

$$= 9x^2 - 12x + 4$$

Outcome 5b

19. Factor the following

Factor by removing the gcf

a) $14a^3b^2 - 28b^3c^2 + 21a^2c^3$

$$7a(2a^2b^2 - 4b^3c^2 + 3a^2c^3)$$

Factor the following. Remember to always remove the gcf first if possible

b) $n^2 - n - 12$

$$(n + 3)(n - 4)$$

c) $36r^2 - 64m^2$

$$= 4(9r^2 - 16m^2)$$

$$= 4(3r + 4m)(3r - 4m)$$

d) $6m^2 + 23m - 18$

$$= (2m + 9)(3m - 2)$$

$\begin{matrix} 2 \times 9 = 18 \\ 3 \times -2 = -6 \\ 18 - 6 = 12 \end{matrix}$

e) $w^2 - 22wx + 121x^2$

$$= (w - 11x)(w - 11x)$$

f) $8m - 4m^2$

$$= 4m(2 - m)$$

g) $-24m^2n - 6mn^2$

$$= -6mn(4m + n)$$

h) $x^2 + 8x + 12$

$$= (x + 6)(x + 2)$$

i) $q^2 + 6q + 8$

$$= (q + 4)(q + 2)$$

j) $u^2 - 12u + 27$

$$= (u - 9)(u - 3)$$

$$k) 6m^2 + 5m - 21$$

$$= (2m - 3)(3m + 7)$$

$$l) 16v^2 - 49$$

$$= (4v + 7)(4v - 7)$$

$$m) 9y^2 - 25x^2$$

$$= (3y + 5x)(3y - 5x)$$

$$n) x^2 - 5x$$

$$= x(x - 5)$$

$$o) 2w^2 + 3w - 20$$

$$= (w + 4)(2w - 5)$$

$$p) 5w^2 + 15w + 10$$

$$= 5(w^2 + 3w + 2)$$

$$= 5(w + 1)(w + 2)$$

$$q) 6x^2 - 13xy - 5y^2$$

$$(2x - 5y)(3x + y)$$

$$r) 3x^2 - 14x + 8$$

$$= (x - 4)(3x - 2)$$

$$s) 16x^4 - 1$$

$$= (4x^2 + 1)(4x^2 - 1)$$

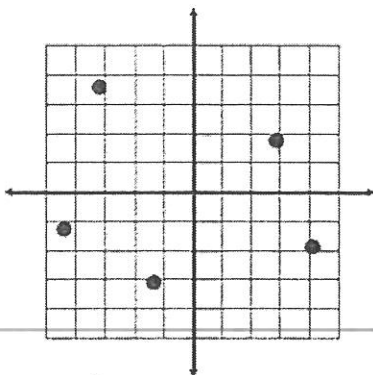
$$= (4x^2 + 1)(2x + 1)(2x - 1)$$

Outcomes 6

Level 2

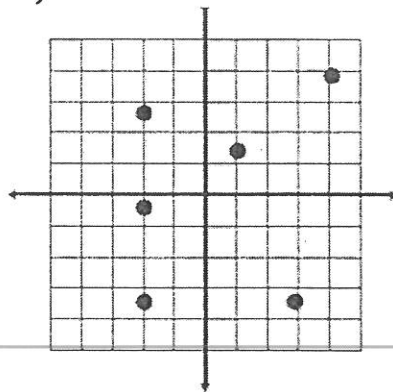
20. Determine if each relation below is a function.

a)



Function

b)



Not a
Function

c)

x	y
8	-3
7	-3
6	-3
5	-3
4	-3

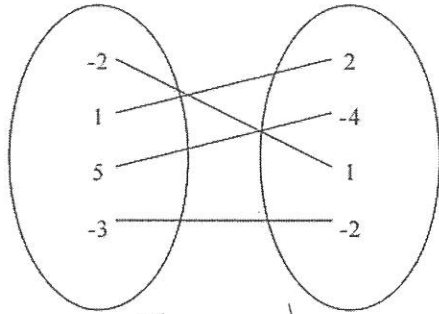
Function

d)

x	y
-2	7
6	4
-1	-2
-2	3

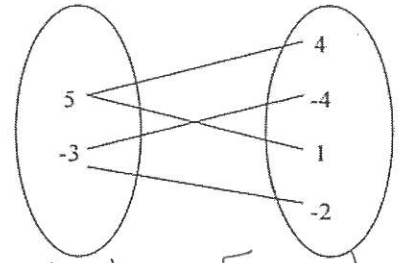
Not a Function

e)



Function

f)



Not a Function

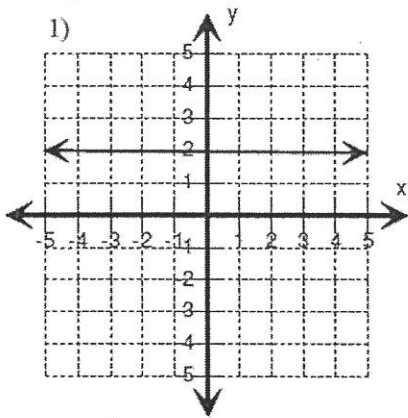
g) $\{(1, 3), (1, 5), (2, 7), (2, 9)\}$

Not a Function

h) $\{(1, 5), (3, 5), (4, 6), (9, 0)\}$

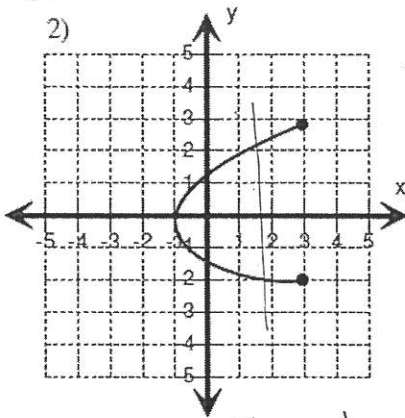
Function

i)



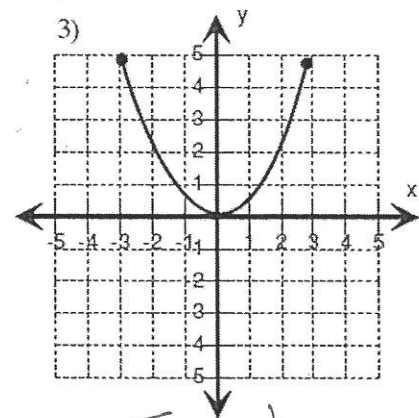
Function

j)



Not a Function

k)



Function.

level 2/3

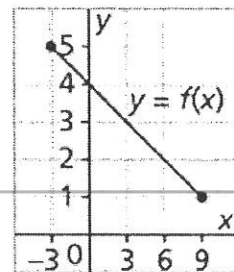
21. State the Domain & Range of the following:

a) $\{(1, 3), (2, 5), (3, 7), (4, 7)\}$

$$D = \{1, 2, 3, 4\}$$

$$R = \{3, 5, 7\}$$

b)



$$D = [-3, 9] \text{ or } \{x \mid -3 \leq x \leq 9, x \in \mathbb{R}\}$$

$$R = [1, 5] \text{ or } \{y \mid 1 \leq y \leq 5, y \in \mathbb{R}\}$$

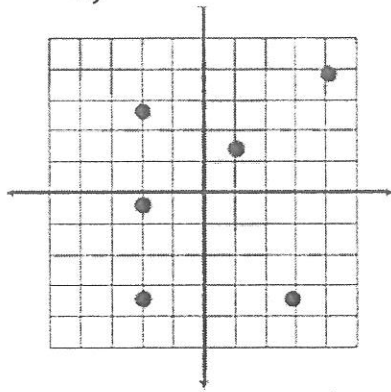
b)

x	y
-2	7
6	4
-1	-2
-2	3

$$D = \{-2, -1, 6\}$$

$$R = \{-2, 3, 4, 7\}$$

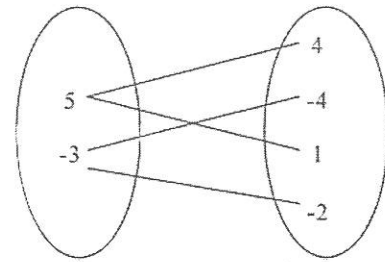
d)



$$D = \{-2, 1, 3, 4\}$$

$$R = \{-3, 5, -0.5, 1.5, 2.5, 4\}$$

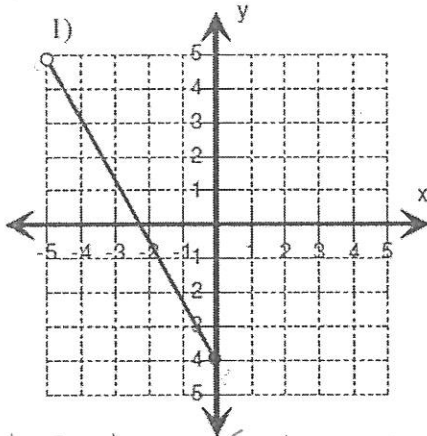
e)



$$D = \{-3, 5\}$$

$$R = \{-4, -2, 1, 4\}$$

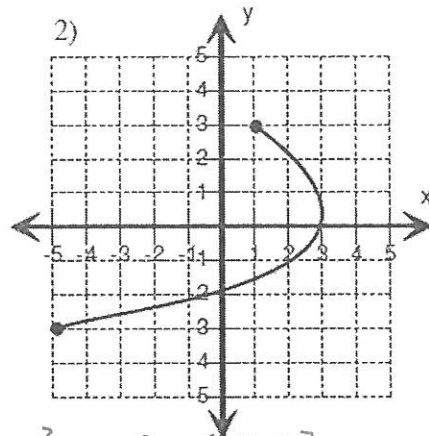
f)



$$D = (-5, 0) \text{ or } \{x \mid -5 < x \leq 0, x \in \mathbb{R}\}$$

$$R = [-4, 5) \text{ or } \{y \mid -4 \leq y < 5, y \in \mathbb{R}\}$$

g)



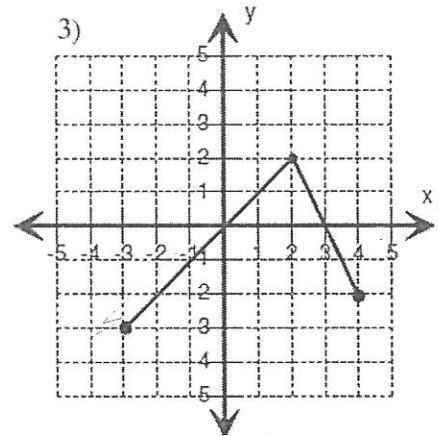
$$D = [-5, 3]$$

$$\text{or } \{x \mid -5 \leq x < 3, x \in \mathbb{R}\}$$

$$R = [-3, 3]$$

$$\text{or } \{y \mid -3 \leq y \leq 3, y \in \mathbb{R}\}$$

h)



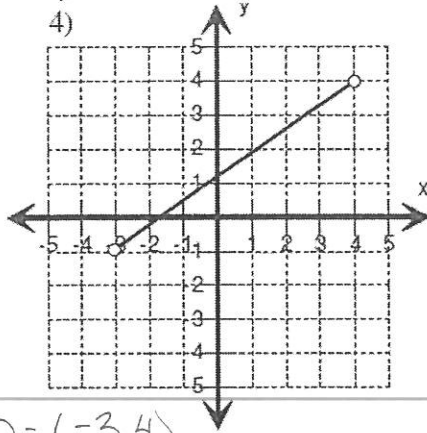
$$D = [-3, 4]$$

$$\text{or } \{x \mid -3 \leq x \leq 4, x \in \mathbb{R}\}$$

$$R = [-3, 2]$$

$$\text{or } \{y \mid -3 \leq y \leq 2, y \in \mathbb{R}\}$$

i)



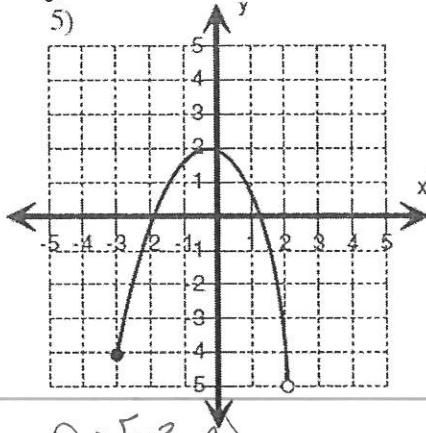
$$D = (-3, 4)$$

$$\text{or } \{x \mid -3 < x < 4, x \in \mathbb{R}\}$$

$$R = (-1, 4)$$

$$\text{or } \{y \mid -1 < y < 4, y \in \mathbb{R}\}$$

j)



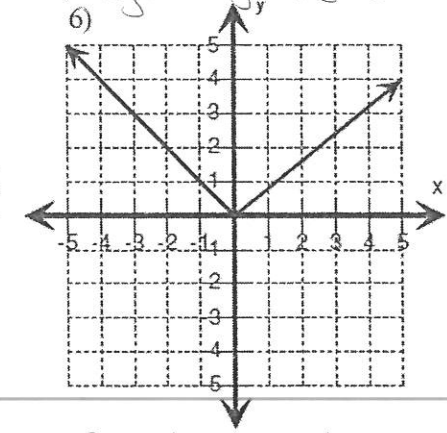
$$D = [-3, 2)$$

$$\{x \mid -3 \leq x < 2, x \in \mathbb{R}\}$$

$$R = (-5, 2]$$

$$\{y \mid -5 < y \leq 2, y \in \mathbb{R}\}$$

k)



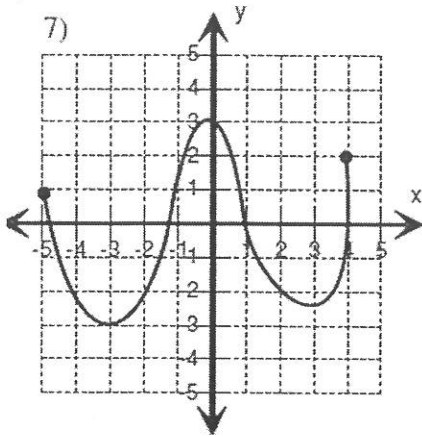
$$D = (-\infty, \infty)$$

$$\{x \in \mathbb{R}\}$$

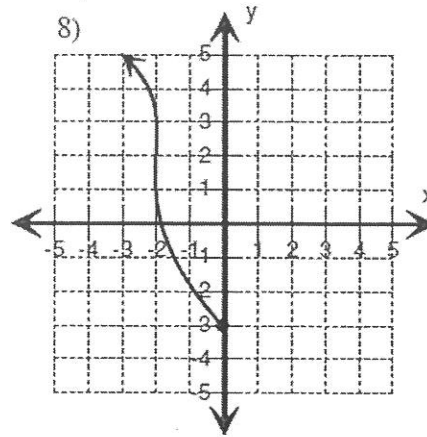
$$R = [0, \infty)$$

$$\{y \mid y \geq 0, y \in \mathbb{R}\}$$

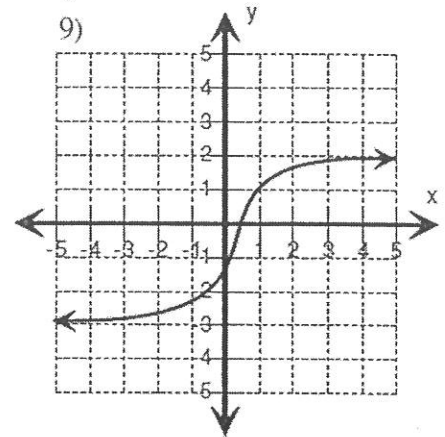
l)



m)



n)



Outcome 7

22. Determine the slope of a line for each equation

a) $y = -2x + 7$

$m = -2$

b) $y + 7 = 3(x - 8)$

$m = 3$

c) $y = 9 - 5x$

$m = -5$

d) $y = x$

$m = 1$

23. A line has slope $\frac{3}{5}$

a) What is the slope of a line that is parallel to this one?

$\frac{3}{5}$

b) What is the slope of a line that is perpendicular to this one?

$-\frac{5}{3}$

24. A line has a slope of -4.

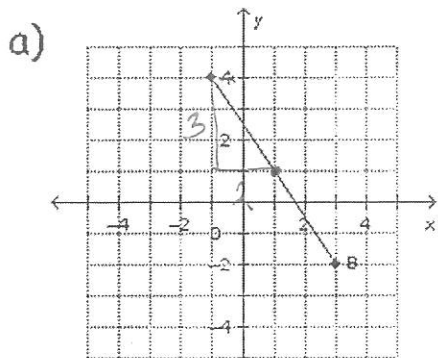
c) What is the slope of a line that is parallel to this one?

-4

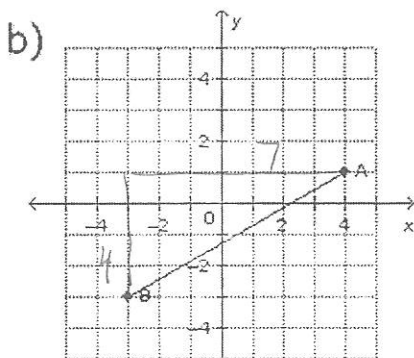
d) What is the slope of a line that is perpendicular to this one?

$\frac{1}{4}$

25. Determine the slope from the following graphs.



$$m = -\frac{3}{2}$$



$$m = \frac{4}{7}$$

Level 3

26. Determine the slope of a line that passes through the following points.

a) $(-6, 8)$ and $(-1, -2)$

$$\begin{aligned} m &= \frac{-2-8}{-1-(-6)} \\ &= \frac{-10}{5} \\ &= -2 \end{aligned}$$

b) $(-3, 7)$ and $(5, -5)$

$$\begin{aligned} m &= \frac{-5-7}{5-(-3)} \\ &= \frac{-12}{8} \\ &= -\frac{3}{2} \end{aligned}$$

27. The equations of two lines are given. Are the two lines parallel, perpendicular or neither? Explain your reasoning.

a) $y = -3x + 6$

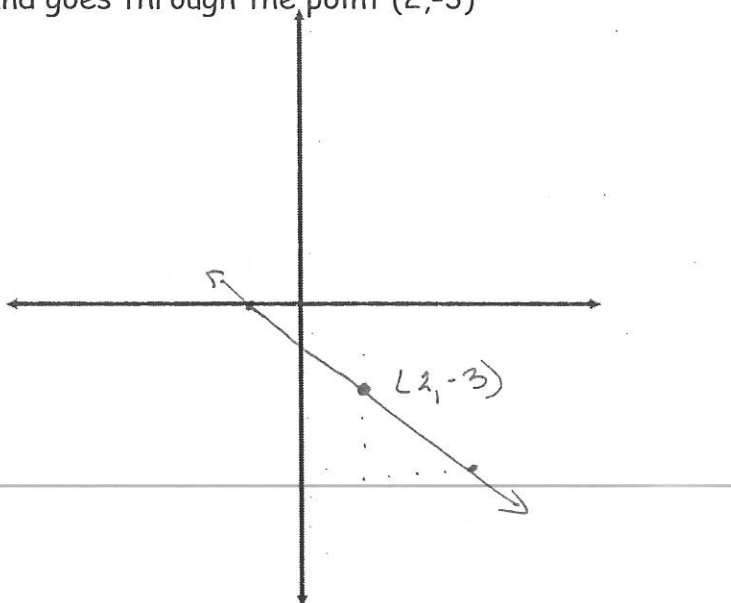
$y = \frac{1}{3}x - 20$

Perpendicular

$m = -3$ $m = \frac{1}{3}$

Negative reciprocals

28. Draw a line segment that has a slope of $-\frac{3}{4}$ and goes through the point $(2, -3)$



Outcome 8a

Level 2

29. State whether the following represent a linear relation.

a) $2x + 3y = 7$

Yes

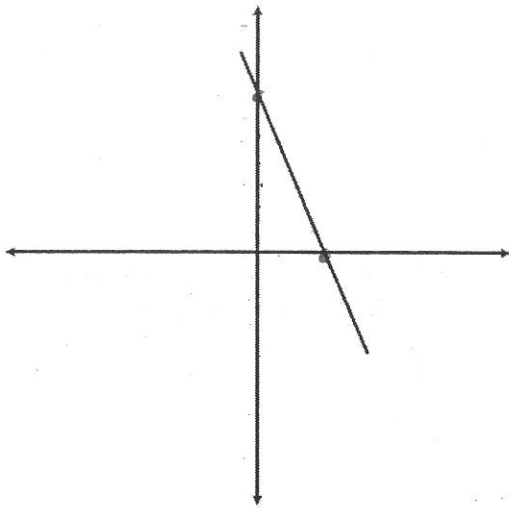
b) $\{(2,7), (4,10), (6,13), (8,16)\}$

Yes

c) $x = -4$

Yes

30. What are the coordinates of the:



x intercept: $(3, 0)$

y intercept: $(7, 0)$

Level 3

31. If $g(x) = 2x - 4$, determine:

a) $g(-1)$

$$g(-1) = 2(-1) - 4$$

$$g(-1) = -2 - 4$$

$$g(-1) = -6$$

b) x if $g(x) = 2$

$$2 = 2x - 4$$

$$6 = 2x$$

$$x = 3$$

32. Calculate the x and y intercepts for each of the equations:

a) $2x - 5y = 20$

x-int

$$2x - 5(0) = 20$$

$$2x = 20$$

$$x = 10$$

y-int

$$2(0) - 5y = 20$$

$$-5y = 20$$

$$y = -4$$

2) $7y + 4x + 56 = 0$

x-int

$$7(0) + 4x + 56 = 0$$

$$4x = -56$$

$$x = -14$$

y-int

$$7y + 4(0) + 56 = 0$$

$$7y = -56$$

$$y = -8$$

Outcome 8b

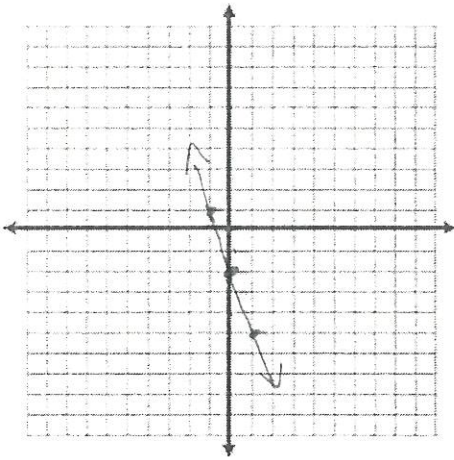
Level 3

33. Graph the following equations

a) $y = -3x - 2$

$$m = -\frac{3}{1}$$

$$y\text{-int} = -2$$

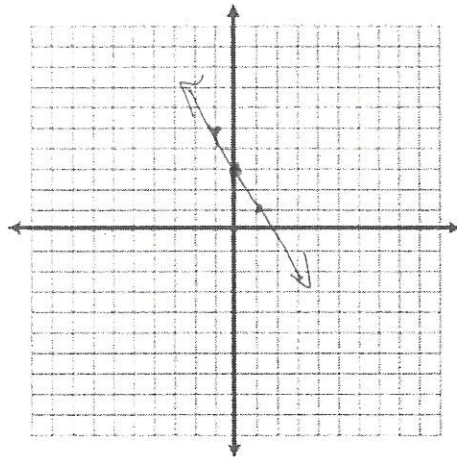


b) $2x + y - 3 = 0$

$$y = -2x + 3$$

$$m = -2$$

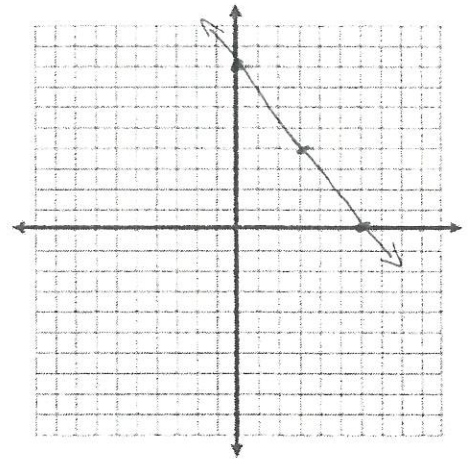
$$y\text{-int} = 3$$



c) $4x + 3y - 24 = 0$

$$3y = -4x + 24$$

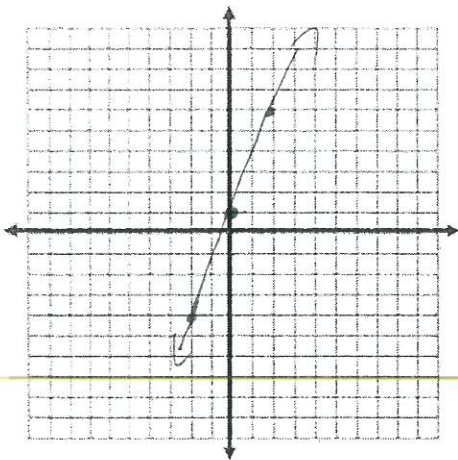
$$y = -\frac{4}{3}x + 8$$



d) $y = \frac{5}{2}x + 1$

$$m = \frac{5}{2}$$

$$y\text{-int} = 1$$



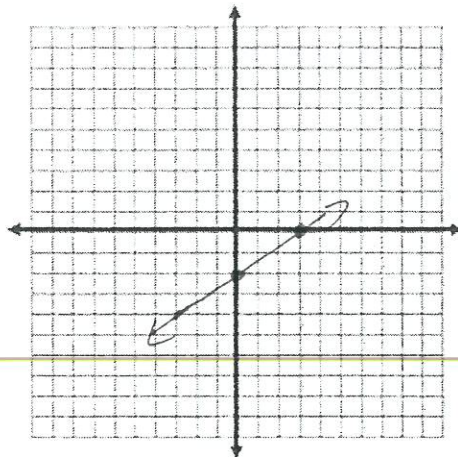
e) $2x - 3y = 6$

$$-3y = -2x + 6$$

$$y = \frac{2}{3}x - 2$$

$$m = \frac{2}{3}$$

$$y\text{-int} = -2$$



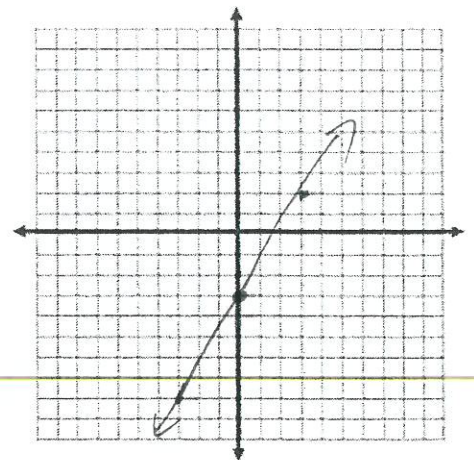
f) $-5x + 3y + 9 = 0$

$$3y = 5x - 9$$

$$y = \frac{5}{3}x - 3$$

$$m = \frac{5}{3}$$

$$y\text{-int} = -3$$



Outcome 9

Level 2

34. Write an equation of a line that has a slope of -4 and a y-intercept of 9 .

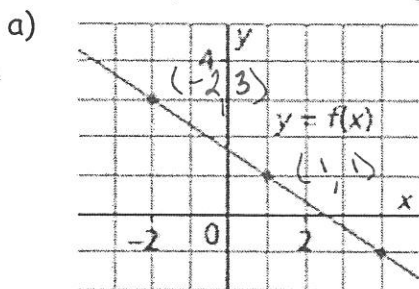
$$y = -4x + 9$$

35. Write an equation of a line that has a slope of $\frac{-2}{3}$ and passes through the point $(-2, 5)$.

$$y - 5 = \frac{-2}{3}(x + 2)$$

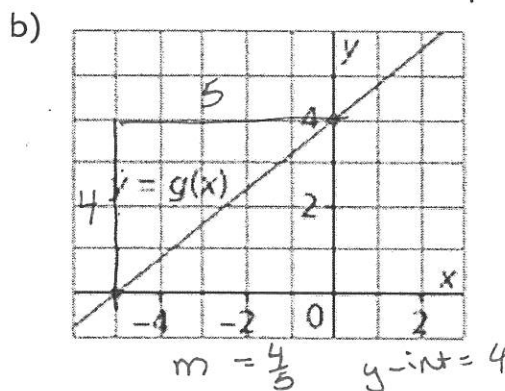
Level 3

36. Write an equation for each graph. Do not use estimates in our equations.



$$m = \frac{3-1}{-2-1} = \frac{2}{-3}$$

$$y - 3 = \frac{-2}{3}(x + 2)$$



$$m = \frac{4}{5} \quad y\text{-int} = 4$$

$$y = \frac{4}{5}x + 4$$

37. Write an equation in slope-intercept form that:

a) has slope 3 and passes through $M(2, -5)$

$$y + 5 = 3(x - 2)$$

$$y + 5 = 3x - 6$$

$$y = 3x - 11$$

b) has slope -4 and passes through $N(1, 4)$

$$y = -4x + b$$

$$4 = -4(1) + b$$

$$8 = b$$

$$y = -4x + 8$$

c) passes through $(-3, 5)$ and $(-1, 2)$

$$m = \frac{2-5}{-1-(-3)} = \frac{-3}{2}$$

$$y-2 = \frac{-3}{2}(x+1)$$

$$y-2 = \frac{-3}{2}x - \frac{3}{2}$$

$$y = \frac{-3}{2}x + \frac{1}{2}$$

d) is parallel to $y = -\frac{1}{3}x - 7$ and has an x-intercept of -3

$$m = -\frac{1}{3}$$

$(-3, 0)$

$$y = -\frac{1}{3}x + b$$

$$0 = -\frac{1}{3}(-3) + b$$

$$0 = 1 + b$$

$$-1 = b$$

$$y = -\frac{1}{3}x - 1$$

38. Write an equation in general form that:

a) passes through the points $(2, 3)$ and $(-4, 5)$

$$m = \frac{5-3}{-4-2} = \frac{2}{-6} = -\frac{1}{3}$$

$$y-5 = \frac{-1}{3}(x+4)$$

$$\begin{array}{l} \times 3 \\ 3y - 15 = -1(x+4) \end{array}$$

$$\begin{array}{l} \times 3 \\ 3y - 15 = -x - 4 \end{array}$$

$$\rightarrow x + 3y - 11 = 0$$

b) passes through the points $(1, 4)$ and $(5, 6)$

$$m = \frac{6-4}{5-1} = \frac{2}{4} = \frac{1}{2}$$

$$y-4 = \frac{1}{2}(x-1)$$

$$\begin{array}{l} \times 2 \\ 2y - 8 = 1(x-1) \end{array}$$

$$2y - 8 = x - 1$$

$$\rightarrow x - 2y + 7 = 0$$

c) has slope 2 and passes through $(3, 6)$

~~$$y = 2x + b$$~~

$$y-6 = 2(x-3)$$

$$y-6 = 2x-6$$

$$0 = 2x - y$$

d) has a slope of $\frac{2}{3}$ and passes through $(-1, 4)$

$$\begin{array}{r} y - 4 = \frac{2}{3}(x + 1) \\ \times 3 \quad \times 3 \quad \times 3 \end{array}$$

$$3y - 12 = 2(x + 1)$$

$$3y - 12 = 2x + 2$$

$$0 = 2x - 3y + 14$$

e) is perpendicular to $y - 4 = 2(x + 7)$ and passes through the point $(-3, -5)$

$$m = -\frac{1}{2}$$

$$\begin{array}{r} y + 5 = -\frac{1}{2}(x + 3) \\ \times 2 \quad \times 2 \quad \times 2 \end{array}$$

$$2y + 10 = -1(x + 3)$$

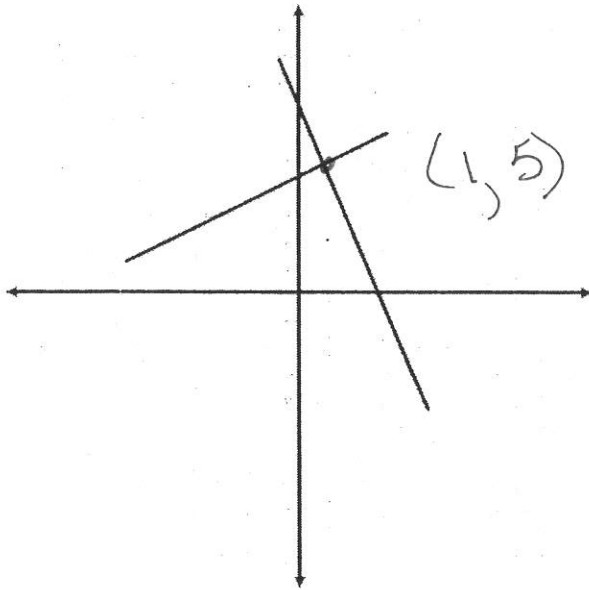
$$2y + 10 = -x - 3$$

$$x + 2y + 13 = 0$$

Outcome 10

Level 2/3

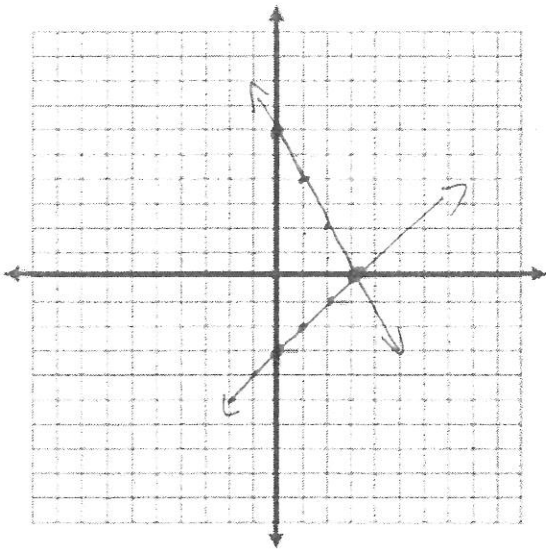
39. Determine the solution to the system of equations.



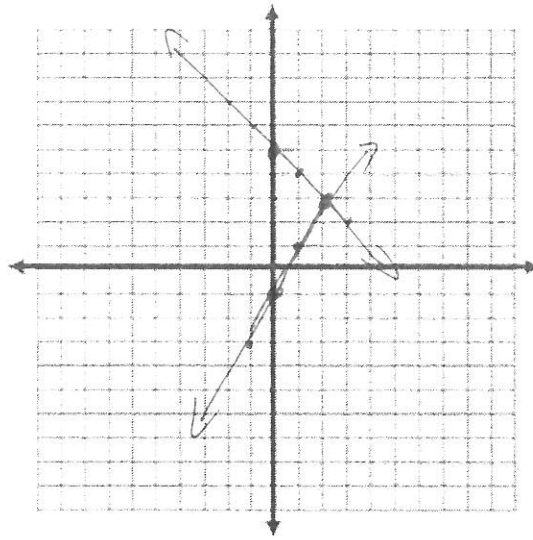
40. Solve the following systems graphically.

a) $x - y = 3$ $y = x - 3$
 $2x + y = 6$ $y = -2x + 6$

b) $y = -x + 5$
 $y = 2x - 1$



$(3, 0)$



$(2, 3)$

41. Solve the following systems using substitution

a) $x + y = -5$ $x = -y - 5$
 $x + 3y = -15$

$-y - 5 + 3y = -15$

$2y = -10$

$y = -5$

$x = -(-5) - 5$

$x = 0$

$(0, -5)$

b) $4x + y = -5$ $y = -4x - 5$
 $2x + 3y = 5$

$2x + 3(-4x - 5) = 5$

$2x - 12x - 15 = 5$

$-10x = 20$

$x = -2$

$y = -4(-2) - 5$

$y = 8 - 5$

$y = 3$

$(-2, 3)$

c) $7x + y - 10 = 0$ $y = -7x + 10$
 $3x - 2y = -3$

$3x - 2(-7x + 10) = -3$

$3x + 14x - 20 = -3$

$17x = 17$

$x = 1$

$y = -7(1) + 10$

$y = 3$

$(1, 3)$

42. Solve the following systems using elimination

$$\begin{aligned} \text{a) } & -3x - y = 5 \\ & + (2x + y = -5) \end{aligned}$$

$$-x = 0$$

$$x = 0$$

$$2(0) + y = -5$$

$$y = -5$$

$$(0, -5)$$

$$\text{b) } \begin{aligned} & 2x - 4y = 13 \times 2 \\ & (4x - 5y = 8) \end{aligned}$$

$$-(4x - 8y = 26)$$

$$3y = -18$$

$$y = -6$$

$$2x - 4(-6) = 13$$

$$2x + 24 = 13$$

$$2x = -11$$

$$x = -\frac{11}{2}$$

$$\left(-\frac{11}{2}, -6\right)$$

$$\begin{aligned} \text{c) } & -0.5x + 0.2y = -1 \times 3 \\ & (0.3x - 0.6y = -1.8) \\ & + (-1.5x + 0.6y = -3) \end{aligned}$$

$$-1.2x = -4.8$$

$$x = 4$$

$$-0.5(4) + 0.2y = -1$$

$$-2 + 0.2y = -1$$

$$0.2y = 1$$

$$y = 5$$

$$(4, 5)$$

43. Determine the number of solutions of each system

$$\begin{aligned} \text{a) } & y = 3x - 2 \\ & y = -4x + 5 \end{aligned}$$

1

$$\begin{aligned} \text{b) } & 4x - 2y = -0.2 \\ & -x + 0.5y = 0.05 \end{aligned}$$

$$-2y = -4x - 0.2$$

$$y = 2x + 0.1$$

$$0.5y = x + 0.05$$

$$y = 2x + 0.1$$

Infinite

$$\begin{aligned} \text{c) } & y = 3x - 2 \\ & y = 3x + 2 \end{aligned}$$

0

44. Determine if each point is a solution to the system.

$$\text{a) } (-2, 3)$$

$$2x - y = -7$$

$$3x + y = 7$$

$$2(-2) - 3 = -7$$

$$-4 - 3 = -7$$

$$-7 = -7 \checkmark$$

$$3(-2) + 3 = 7$$

$$-6 + 3 = 7$$

$$-3 = 7 \times$$

No

$$\text{b) } (1, -1)$$

$$3x - 4y = 7$$

$$9x + 6y = 3$$

$$3(1) - 4(-1) = 7$$

$$3 + 4 = 7$$

$$7 = 7 \checkmark$$

$$9(1) + 6(-1) = 3$$

$$9 - 6 = 3$$

$$3 = 3 \checkmark$$

Yes

$$\text{d) } (4, -3)$$

$$2x - y = 11$$

$$x + 2y = -2$$

$$2(4) - (-3) = 11$$

$$8 + 3 = 11$$

$$11 = 11 \checkmark$$

$$4 + 2(-3) = -2$$

$$4 - 6 = -2$$

$$-2 = -2 \checkmark$$

Yes